# Nucleon electromagnetic structure: Past, present, and future 

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#### Abstract

Summary. - We present the experimental status of electromagnetic hadron form factors. New and surprising results, based on polarization measurements, have been recently obtained for the electric proton and neutron form factors. In particular, the electric and magnetic distributions inside the proton appear not to be the same, in disagreement with results extracted from the unpolarized cross-section, using the Rosenbluth separation. The new findings have given rise to a large number of papers and different speculations, as they question directly the models of nucleon structure and the reaction mechanism itself (based on $1 \gamma$-exchange), with a possible revision of the calculation of radiative corrections, two-photon contribution, etc. New data in time-like region are also available, through annihilation reactions. A large interest in this field arises, due also to the possibility of new measurements in polarized electron nucleon elastic scattering at JLab, and also in the time-like region, at Frascati and at the future FAIR international facility.


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PACS 13.40.Gp - Electromagnetic form factors.

## 1. - Introduction

Form factors (FFs) characterize the internal structure of composite particles. They constitute a convenient playground for theory and experiment, because, on the one side, they are directly related to experimental observables as cross-sections and polarization observables, and, on the other side, they enter in the expression of the nucleon electromagnetic current, calculable by the models which describe the nucleon structure.

In a $P$ - and $T$-invariant theory, a particle with spin $S$ is characterized by $2 S+1$ electromagnetic form factors. The nucleon has two FFs, called electric ( $G_{\mathrm{EN}}$ ) and magnetic $\left(G_{\mathrm{MN}}\right)$, which, a priori, are different. Proton and neutron FFs are also different.

Electromagnetic probes are traditionally preferred to the hadronic beams, and elastic electron hadron scattering contains all information on the nucleon ground state. The reaction mechanism is assumed to be one-photon exchange, the electromagnetic interaction is exactly calculable in QED, and one can safely extract the information on the hadronic vertex. However, one has to introduce radiative corrections, which become very large
as the momentum transfer squared, $Q^{2}$, increases. Radiative corrections were firstly calculated by Schwinger [1] and are important for the discussion of the experimental determination of the differential cross-section. They are also calculable in QED.

The four-momentum transfer squared transmitted to the virtual photon, $q^{2}=-Q^{2}=$ $-4 E E^{\prime} \sin ^{2}\left(\theta_{\mathrm{e}} / 2\right)$ (where $E$ and $E^{\prime}$ are the energies of the incident and scattered electron, and $\theta_{\mathrm{e}}$ is the electron scattering angle in Lab system), is negative in elastic eh scattering, i.e. the space component is larger than the time component. The accessible kinematical region is called space-like (SL) region. Annihilation reactions, such as $\mathrm{N}+\overline{\mathrm{N}} \leftrightarrow \ell^{+}+\ell^{-}$, $\ell=\mu$ or e, allow to scan the time-like (TL) region, $q^{2}>4 m^{2}$, where $m$ is the nucleon mass. The relevant variable in TL region is the square of the total energy, $s=q^{2}$.

Form factors are analytical functions of $q^{2}$, being real functions in the SL region (due to the hermiticity of the electromagnetic Hamiltonian) and complex functions in the TL region. The Phràgmen-Lindelöf theorem [2] gives a rigorous prescription for the asymptotic behavior of analytical functions: $\lim _{q^{2} \rightarrow-\infty} F^{(\mathrm{SL})}\left(q^{2}\right)=\lim _{q^{2} \rightarrow \infty} F^{(\mathrm{TL})}\left(q^{2}\right)$. This means that, asymptotically, FFs, have the following constraints: 1) the time-like phase vanishes and 2) the real part of FFs, $\mathcal{R e} F^{(\mathrm{TL})}\left(q^{2}\right)$, coincides with the corresponding value, $F^{(\mathrm{SL})}\left(q^{2}\right)$.

These asymptotic properties based on analiticity, however, are different from the asymptotics properties of FFs, predicted in QCD, which derive from scaling rules and helicity conservation. Therefore, the study of FFs at large $Q^{2}$ represents a unique tool for the understanding of these properties of the nucleon dynamics.

## 2. - The past

The importance of FFs was recognized since the first measurements of R. Hofstadter [3], Nobel laureate in 1961, to whom G. Liljestrand, member of the Royal Academy of Sciences, addressed with these words: "The myth of the indivisibility of the atom, implied in its very name, was shattered in the beginning of this century, and a completely new and fascinating world of the utmost importance became revealed. You have been able to obtain further significant information of the intimate structure of this intriguing world by disclosing the distribution of electric charges and magnetic forces within the atomic nucleus, and the particles of which it is composed."

An elegant formalism, in QED, allows to relate measured quantities, as cross-section and polarization observables to FFs. The expressions which relate the moduli of FFs to the unpolarized differential cross-section were developed by Rosenbluth [4] for the scattering channel, $e+N \rightarrow e+N$, and, for the annihilation channel, by Zichichi, Berman, Cabibbo and Gatto [5]. The importance of polarization phenomena, and the related formalism, were firstly suggested by the "Kharkov school" of Akhiezer and Rekalo [6], and, in TL region, by Bilenkyi, Giunti and Wataghin [7] and Dubnickova, Rekalo and Dubnicka [8].

The comparison of the observables with the theoretical models of hadron structure is straightforward, as, in framework of the mechanism of one-photon approximation, FFs enter directly in the expression of the hadronic electromagnetic current. The matrix element of the process $\mathrm{e}+\mathrm{N} \rightarrow \mathrm{e}+\mathrm{N}$ is written as

$$
\begin{equation*}
\mathcal{M}_{1}=\frac{e^{2}}{Q^{2}} \bar{u}\left(k_{2}\right) \gamma_{\mu} u\left(k_{1}\right) \bar{u}\left(p_{2}\right)\left[F_{1 \mathrm{~N}}\left(Q^{2}\right) \gamma_{\mu}-\frac{\sigma_{\mu \nu} q_{\nu}}{2 m} F_{2 \mathrm{~N}}\left(Q^{2}\right)\right] u\left(p_{1}\right), \tag{1}
\end{equation*}
$$

where $k_{1}\left(p_{1}\right)$ and $k_{2}\left(p_{2}\right)$ are the four-momenta of the initial and final electron (nucleon),
$q=k_{1}-k_{2}, Q^{2}=-q^{2}>0 . F_{1 \mathrm{~N}}$ and $F_{2 \mathrm{~N}}$ are the Dirac and Pauli nucleon electromagnetic form factors. The same FFs enter also in the description of elastic scattering of positrons by nucleons. From eq. (1) one can find the following expression for the differential crosssection in the laboratory system:

$$
\begin{equation*}
\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega_{\mathrm{e}}}=\sigma_{0}\left[G_{\mathrm{MN}}^{2}\left(Q^{2}\right)+\frac{\epsilon}{\tau} G_{\mathrm{EN}}^{2}\left(Q^{2}\right)\right], \tau=Q^{2} /\left(4 m^{2}\right), \tag{2}
\end{equation*}
$$

where $\sigma_{0}$ is a kinematical factor, which contains the Mott cross-section, for the scattering of unpolarized electrons by a point charge particle (with spin $1 / 2$ ), $\epsilon$ is the second independent kinematical variable, which, together with $Q^{2}$, fully determines the kinematics of elastic eN-scattering and can be written, in the zero electron mass limit, as

$$
\begin{equation*}
\epsilon=\left[1+2(1+\tau) \tan ^{2} \frac{\theta_{\mathrm{e}}}{2}\right]^{-1}, 0 \leq \epsilon \leq 1 . \tag{3}
\end{equation*}
$$

The Sachs FFs $G_{\mathrm{MN}}$ and $G_{\mathrm{EN}}$ are related to the Dirac and Pauli FFs by: $G_{\mathrm{MN}}=$ $F_{1 \mathrm{~N}}+F_{2 \mathrm{~N}}$, and $G_{\mathrm{EN}}=F_{1 \mathrm{~N}}-\tau F_{2 \mathrm{~N}}$. From eq. (2) it appears that the cross-section depends linearly on $\epsilon$, and measurements at fixed $Q^{2}$, at different angles, allow a straightforward extraction of the electric and magnetic FFs. However, as $Q^{2}$ increases, the electric contribution becomes small, compared to the magnetic part, which is weighted by the factor $\tau$. Its precise determination becomes, therefore, more difficult.

Taking a longitudinally polarized electron beam, and measuring the polarization of the outgoing proton, in $\vec{e}+p \rightarrow e+\vec{p}$ (or, alternatively, using a polarized target, with longitudinally polarized beam), the polarization induces an interference term, in the cross-section, related to the product of $G_{\mathrm{MN}}$ and $G_{\mathrm{EN}}$. It has been shown that the transverse $\left(P_{\mathrm{T}}\right)$ and the longitudinal $\left(P_{\mathrm{L}}\right)$ polarization of the proton in the reaction plane (the third component, normal to the scattering plane vanishes, due to $T$-invariance) are proportional to $G_{\mathrm{Ep}} G_{\mathrm{Mp}}$ and $G_{\mathrm{Mp}}^{2}$, respectively, so that the simultaneous measurement of these two polarization components gives directly the ratio of the form factors:

$$
\begin{equation*}
\frac{G_{\mathrm{Ep}}}{G_{\mathrm{Mp}}}=-\frac{P_{\mathrm{T}}}{P_{\mathrm{L}}} \frac{\left(E+E^{\prime}\right)}{2 m} \tan \frac{\theta_{\mathrm{e}}}{2} . \tag{4}
\end{equation*}
$$

The experimental realization of this method requires a polarized beam with high intensity, as the proton polarization has to be measured through a secondary scattering on a carbon or polyethylene target. This is the reason for which it has become possible only in the recent years.

## 3. - The present

3. Space-like region. - In SL region, the measurements based on the Rosenbluth method show that the behavior of the magnetic proton and neutron FFs as a function of $Q^{2}$, follows approximately a dipole law:

$$
\begin{equation*}
G_{\mathrm{MN}}\left(Q^{2}\right) / \mu_{\mathrm{N}}=G_{\mathrm{d}}, \text { with } G_{\mathrm{d}}=\left[1+Q^{2} / m_{\mathrm{d}}^{2}\right]^{-2}, m_{\mathrm{d}}^{2}=0.71 \mathrm{GeV}^{2}, \tag{5}
\end{equation*}
$$

where $\mu_{\mathrm{N}}$ is the nucleon magnetic moment in units of the Bohr magneton, respectively $\mu_{\mathrm{p}}=2.79$ for proton and $\mu_{\mathrm{n}}=-1.913$ for neutron.

Such behavior is consistent with the scaling laws predicted by QCD [9], but also with a nonrelativistic picture of an exponential distribution of the magnetization inside the nucleon.

Concerning the electric proton FF, when comparing the data derived from the Rosenbluth separation and from the polarization transfer method, it turns out that a discrepancy appears between the $Q^{2}$-dependences of the FFs ratio $R$.

From the Rosenbluth separation data one finds the scaling relation: $R=\mu_{\mathrm{p}} G_{\mathrm{Ep}} / G_{\mathrm{Mp}}$ $\simeq 1$, whereas the following parametrization describes the polarization data $[10,11]$ :

$$
\begin{equation*}
R=\mu_{\mathrm{p}} G_{\mathrm{Ep}} / G_{\mathrm{Mp}}=1-0.13\left(Q^{2}\left[\mathrm{GeV}^{2}\right]-0.04\right) \tag{6}
\end{equation*}
$$

which implies that the ratio monotonically decreases and deviates from unity, as $Q^{2}$ increasing, reaching a value of $R \simeq 0.3$ at $Q^{2}=5.5 \mathrm{GeV}^{2}$.

A careful experimental and theoretical analysis of this problem is necessary. The important point is the calculation of radiative corrections to the differential cross-section and to polarization observables in elastic eN-scattering. If these corrections are large (in absolute value) for the differential cross-section [12], in particular for high-resolution experiments, a simplified estimation of radiative corrections to polarization phenomena [13] shows that radiative corrections are small for the ratio $P_{\mathrm{T}} / P_{\mathrm{L}}$. The possibility of a contribution of two-photon exchange, suggested long ago [14], is actually investigated, and gives rise to experimental $[15,16]$ and theoretical efforts [17, 18].

Experiments, based on the Rosenbluth method have been performed in several laboratories (SLAC, Bonn, DESY, ...), especially at low $Q^{2}$. A recent analysis and exhaustive references on proton FFs experiments can be found in [19].

Experiments, based on the polarization transfer method, have been performed at MAMI, NIKHEF, JLab, $\ldots$ up to $Q^{2}=5.6 \mathrm{GeV}^{2}[10,11]$.

The neutron electric FF is small and the polarization transfer method appears very useful, even at low momentum transfer. Recent measurements, using a polarized target $\left({ }^{3} \mathrm{He}\right.$ or deuterium), or measuring the polarization of the ougoing nucleon ([20] and references herein), have been done up to $Q^{2}=1.8 \mathrm{GeV}^{2}$ and show that $G_{\text {En }}$ is definitely different from zero.

The world data are shown in fig. 1. The proton electric FF data obtained from unpolarized measurements are shown in fig. 1a (stars), whereas the polarization data are shown as solid squares. The discrepancy among the data issued from the two methods appears clearly.

Different models exist for the description of the nucleon structure. We show, here, as an example, predictions from pQCD, from VDM-inspired models [21, 22] and from an empirical fit [23]. For model [21] (dotted line) and for model [23] (dashed line) the parameters are the same as in the original work, but for model [22] (solid line), a better representation could be obtained after a global fit on all data in SL and TL regions. The pQCD prediction, which follows the dipole law (except for $G_{\text {En }}$ ), is shown as dot-dashed line.
3.2. Time-like region. - In TL region, the measurement of the differential cross-section for the processes $\overline{\mathrm{p}}+\mathrm{p} \leftrightarrow \ell^{+}+\ell^{-}$at a fixed value of the square of the total energy $s$ and for two different angles of the scattered particle, $\theta$, allows the separation of the two FFs, $\left|G_{\mathrm{M}}\right|^{2}$ and $\left|G_{\mathrm{E}}\right|^{2}$, and it is equivalent to the Rosenbluth separation for the elastic ep-scattering. This procedure is simpler in TL region, as it requires to change only one kinematical variable, $\cos \theta$, whereas, in SL region, it is necessary to change simultaneously


Fig. 1. - Nucleon form factors in space-like region: a) proton electric FF, scaled by $\mu_{\mathrm{p}} G_{\mathrm{Mp}}$, b) proton magnetic FF, c) neutron electric FF, d) neutron magnetic FF, scaled by $\mu_{\mathrm{n}} G_{\mathrm{Mn}}$. The predictions of the models are drawn: pQCD (dot-dashed line), model from ref. [21] (dashed line), model from ref. [22] (solid line), model from ref. [23] (dotted line).
two kinematical variables: the energy of the initial electron and the electron scattering angle, fixing the momentum transfer squared, $q^{2}$. However, the Rosenbluth separation of the $\left|G_{\mathrm{E}}\right|^{2}$ and $\left|G_{\mathrm{M}}\right|^{2}$ contributions, has not been realized yet due to the limited statistics which is possible to achieve.

In order to determine the form factors [24], the differential cross-section has to be integrated over a wide angular range. One typically assumes that the $G_{\mathrm{E}}$-contribution plays a minor role in the cross-section at large $q^{2}$ and the experimental results are usually given in terms of $\left|G_{\mathrm{M}}\right|$, under the hypothesis that $G_{\mathrm{E}}=0$ or $G_{\mathrm{E}}=G_{\mathrm{M}}$. The first hypothesis is arbitrary. The second hypothesis is strictly valid at threshold only, i.e. for $\tau=1$, but there is no theoretical argument which justifies its validity at any other momentum transfer.

The $\left|G_{\mathrm{M}}\right|^{2}$ values depend, in principle, on the kinematics where the measurement was performed and on the angular range of integration, however it turns out that these two assumptions for $G_{\mathrm{E}}$ lead to values for $\left|G_{\mathrm{M}}\right|$ which differ by $20 \%$ at most.

Few data exist, especially at large $s$, in the TL region, for proton and even less for neutron. FFs in the TL region are larger than the corresponding SL data. This has been considered as a proof of the nonapplicability of the Phràgmen-Lindelöf theorem (up to


Fig. 2. - Form factors in time-like region. Different figures and curves are described in the text.
$s=18 \mathrm{GeV}^{2}$, at least) or as evidence that the asymptotic regime is not reached [7].
The data in TL region, in the hypothesis that $G_{\mathrm{E}}=G_{\mathrm{M}}$ are shown in fig. 2a for the proton and in fig. 2 b for the neutron, together with the predictions of models. Proton FFs have been measured in $p+\bar{p} \rightarrow e^{+}+e^{-}$at CERN and Fermilab, in $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{p}+\overline{\mathrm{p}}$ at Orsay and Frascati [24]. Neutron TL FFs have been measured at Frascati [25].

The extension to TL region of the VDM-inspired models [21, 22] is based on the following relations, which are necessary for the analytical continuation between SL and TL regions:

$$
Q^{2}=-q^{2}=q^{2} e^{-i \pi} \Longrightarrow\left\{\begin{array}{c}
\ln \left(Q^{2}\right)=\ln \left(q^{2}\right)-i \pi  \tag{7}\\
\sqrt{Q^{2}}=e^{\frac{-i \pi}{2}} \sqrt{q^{2}}
\end{array}\right.
$$

The pQCD prediction (5) can be extended in TL region as [9]

$$
\begin{equation*}
\left|G_{\mathrm{M}}\right|=\frac{A}{s^{2} \ln ^{2}\left(s / \Lambda^{2}\right)} \tag{8}
\end{equation*}
$$

where $\Lambda=0.3 \mathrm{GeV}$ is the QCD scale parameter and $A$ is a free parameter. This simple parametrization is taken to be the same for proton and neutron. The best fit is obtained with a parameter $A(p)=56.3$ for proton and $A(n)=77.15$ for neutron. This reflects the fact that in TL region, neutron FFs are larger than for proton, although the errors are also larger. It has been suggested that an $\mathrm{N} \overline{\mathrm{N}}$ bound state just below the $\mathrm{N} \overline{\mathrm{N}}$ threshold could be responsible for this difference [26].

## 4. - The future

In SL region, if the trend suggested by the recent data based on the polarization metod is confirmed, an extension of the measurements planned at JLab up to $9 \mathrm{GeV}^{2}$ will show evidence for a zero crossing of the electric FF, which could even, eventually, become negative [27].

Concerning the neutron, the extension of large $Q^{2}$ of the measurement on the electric FF will confirm or infirm the fact that this quantity is larger than previously assumed.

These "surprises" on the nucleon FFs affect the description of the light nuclei structure, such as deuteron, and demand for a re-evaluation of the role of the different ingredients usually taken to calculate their structure, such as meson exchange current, relativistic corrections... [28].

In TL region, the angular dependence of the differential cross-section for $\overline{\mathrm{p}}+\mathrm{p} \rightarrow$ $\ell^{+}+\ell^{-}$as a function of the angular asymmetry $\mathcal{R}$ is

$$
\begin{equation*}
\frac{\mathrm{d} \sigma}{\mathrm{~d}(\cos \theta)}=\sigma_{0}\left[1+\mathcal{R} \cos ^{2} \theta\right], \mathcal{R}=\frac{\tau\left|G_{\mathrm{M}}\right|^{2}-\left|G_{\mathrm{E}}\right|^{2}}{\tau\left|G_{\mathrm{M}}\right|^{2}+\left|G_{\mathrm{E}}\right|^{2}} \tag{9}
\end{equation*}
$$

where $\sigma_{0}$ is the value of the differential cross-section at $\theta=\pi / 2$.
The angular dependence of the cross-section, eq. (9), results directly from the assumption of one-photon exchange, where the spin of the photon is equal 1 and the electromagnetic hadron interaction satisfies the $C$-invariance. Therefore, the measurement of the differential cross-section at three angles (or more) would also allow to test the presence of $2 \gamma$ exchange [29].

Polarization phenomena will be especially interesting in $\overline{\mathrm{p}}+\mathrm{p} \rightarrow \ell^{+}+\ell^{-}$. For example, the transverse polarization, $P_{y}$, of the proton target (or the transverse polarization of the antiproton beam) results in nonzero analyzing power $[5,7]$ :

$$
\begin{gathered}
\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega}\left(P_{y}\right)=\left(\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega}\right)_{0}\left[1+\mathcal{A} P_{y}\right] \\
\mathcal{A}=\frac{\sin 2 \theta \operatorname{Im} G_{\mathrm{E}}^{*} G_{\mathrm{M}}}{D \sqrt{\tau}}, D=\left|G_{\mathrm{M}}\right|^{2}\left(1+\cos ^{2} \theta\right)+\frac{1}{\tau}\left|G_{\mathrm{E}}\right|^{2} \sin ^{2} \theta .
\end{gathered}
$$

This analyzing power characterizes the $T$-odd correlation $\vec{P} \cdot \vec{k} \times \vec{p}$, where $\vec{k}(\vec{p})$ is the three momentum of the $\overline{\mathrm{p}}$ beam (produced lepton).

The same information can be obtained from the final polarization in $\ell^{+}+\ell^{-} \rightarrow \overrightarrow{\mathrm{p}}+\overline{\mathrm{p}}$, but in this case one has to deal with the problem of hadron polarimetry, in conditions of very small cross-sections. When both colliding particles are polarized, one acccess to nine possible double-spin observables, $A_{a b}$ (where $a$ and $b=x, y, z$ refer to the $a(b)$ component of the target(projectile) polarization) four of which vanish: $A_{x y}=A_{y x}=A_{z y}=A_{y z}=0$. The nonzero components are

$$
\begin{aligned}
& \frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega} A_{x x}=\sin ^{2} \theta\left(\left|G_{\mathrm{M}}\right|^{2}+\frac{1}{\tau}\left|G_{\mathrm{E}}\right|^{2}\right) \mathcal{N} \\
& \frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega} A_{y y}=-\sin ^{2} \theta\left(\left|G_{\mathrm{M}}\right|^{2}-\frac{1}{\tau}\left|G_{\mathrm{E}}\right|^{2}\right) \mathcal{N}
\end{aligned}
$$



Fig. 3. - Polarization observables. Different figures and curves are described in the text.

$$
\begin{aligned}
\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega} A_{z z} & =\left[\left(1+\cos ^{2} \theta\right)\left|G_{\mathrm{M}}\right|^{2}-\frac{1}{\tau} \sin ^{2} \theta\left|G_{\mathrm{E}}\right|^{2}\right] \mathcal{N} \\
\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega} A_{x z} & =\frac{\mathrm{d} \sigma}{\mathrm{~d} \Omega} A_{z x}=\frac{1}{\sqrt{\tau}} \sin 2 \theta \operatorname{Re} G_{\mathrm{E}} G_{\mathrm{M}}^{*} \mathcal{N}
\end{aligned}
$$

where $\mathcal{N}=\frac{\alpha^{2}}{4 \sqrt{t\left(t-4 m^{2}\right)}}, \alpha=e^{2} /(4 \pi) \simeq 1 / 137$ is a kinematical factor. The predictions for TL observables are shown in fig. 3 for the models described above: the cross-section asymmetry, the single-spin asymmetry, $A$ (fig. 3a), the angular asymmetry, $\mathcal{R}$ (fig. 3d), and the double-spin polarizations $A_{x x}$ (fig. 3b), $A_{y y}$ (fig. 3c), $A_{z z}$ (fig. 3e) and $A_{x z}$ (fig. 3f). For all these observables a large difference appears according to the different models, which qualitatively describe the available SL and TL data. In particular, even the sign can be opposite for VDM-inspired models and pQCD. The model [22] is somehow intermediate between the two representations, as it includes the asymptotic predictions of QCD, at the expenses of a larger number of parameters. It is important to note that the $\tau$-dependence of $\mathcal{A}$ is very sensitive to existing models of the nucleon FFs, which reproduce equally well the data in SL region [30].

## 5. - Conclusions

The field and the formalism of nucleon electromagnetic FFs, developed a few decades ago, are still a source of very interesting developments.

A unique and satisfactory interpretation of the four nucleon FFs (electric and magnetic, for neutron and proton) in TL and SL momentum transfer region has not yet been reached.

In SL region the precise determination of proton and neutron FFs at large-momentum transfer will further strongly constrain the models on light-nuclei structure.

Interesting problems will be addressed and solved by future measurements in TL region:

- the separation of the electric and magnetic FFs, through the angular distribution of the produced leptons: an interesting observable is the measurement of the asymmetry $\mathcal{R}$ (from the angular dependence of the differential cross-section for $\left.\overline{\mathrm{p}}+\mathrm{p} \leftrightarrow \ell^{+}+\ell^{-}\right)$which is sensitive to the relative value of $G_{\mathrm{M}}$ and $G_{\mathrm{E}}$ and does not require polarization observables.
- The presence of a large relative phase of magnetic and electric proton FFs in the TL region, if experimentally proved at relatively large-momentum transfer using polarized target (or beam), will be a strong indication that these FFs have a different behavior.
- The study of the processes $\overline{\mathrm{p}}+\mathrm{p} \rightarrow \pi^{0}+\ell^{+}+\ell^{-}$and $\overline{\mathrm{p}}+\mathrm{p} \rightarrow \pi^{+}+\pi^{-}+\ell^{+}+\ell^{-}$, will allow to measure proton FFs in the TL region, for $s \leq 4 m^{2}$, where the vector meson contribution plays an important role.

It will be possible, in near future, to achieve a new level of precision and also to explore kinematical regions where data are totally absent. This program is especially interesting with respect to the important problem of the transition to the asymptotic region, predicted by QCD, which actually gives rise to many discussions and speculations. FFs should sign unambiguosly the "transition region", where quarks degrees of freedom should be taken explicitly into account and the description of the nucleon, in terms of meson and effective degrees of freedom, no longer holds.

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## REFERENCES

[1] Schwinger J. S., Phys. Rev., 76 (1949) 790.
[2] Titchmarsh E. C., Theory of Functions (Oxford University Press, London) 1939.
[3] Hofstadter R., Bumiller F. and Yearian M., Rev. Mod. Phys., 30 (1958) 482.
[4] Rosenbluth M. N., Phys. Rev., 79 (1950) 615.
[5] Zichichi A., Berman S. M., Cabibbo N. and Gatto R., Nuovo Cimento, XXIV (1962) 170.
[6] Akhiezer A. and Rekalo M. P., Dokl. Akad. Nauk USSR, 180 (1968) 1081; Sov. J. Part. Nucl., 4 (277) 1974.
[7] Bilenky S. M., Giunti C. and Wataghin V., Z. Phys.C, 59 (1993) 475.
[8] Dubnickova A. Z., Rekalo M. P. and Dubnicka S., Z. Phys. C, 70 (1996) 473.
[9] Lepage G. P. and Brodsky S. J., Phys. Rev. D, 22 (1980) 2157; Phys. Rev. Lett., 43 (1979) 545; Phys. Rev. Lett., 43 (1979) 1625 (Erratum).
[10] Jefferson Lab Hall A Collaboration (Jones M. K. et al.), Phys. Rev. Lett., 84 (2000) 1398.
[11] Jefferson Lab Hall A Collaboration (Gayou O. et al.), Phys. Rev. Lett., 88 (2002) 092301.
[12] Mo L. W. and Tsai Y. S., Rev. Mod. Phys., 41 (1969) 205.
[13] L. C. Maximon and J. A. Tjon, Phys. Rev. C, 62 (2000) 054320; Afanasev A., Akushevich I. and Merenkov N., Phys. Rev. D, 64 (2001) 113009; Afanasev A. V., Akushevich I., Ilyichev A. and Merenkov N. P., Phys. Lett. B, 514 (2001) 269.
[14] Gunion J. and Stodolsky L., Phys. Rev. Lett., 30 (1973) 345; Franco V., Phys. Rev. D, 8 (1973) 826; Boitsov V. N., Kondratyuk L. A. and Kopeliovich V. B., Sov. J. Nucl. Phys., 16 (1973) 237; Lev F. M., Sov. J. Nucl. Phys., 21 (1973) 45.
[15] Gilman R., Pentchev L., Perdrisat C. F. and Suleiman R., Jlab Proposal 04-019 (2004).
[16] Arrington J. et al., arXiv:nucl-ex/0408020.
[17] Blunden P. G., Melnitchouk W. and Tjon J. A., Phys. Rev. Lett., 91 (2003) 142304; Guichon P. A. M. and Vanderhaeghen M. , Phys. Rev. Lett., 91 (2003) 142303; Chen Y. C., Afanasev A., Brodsky S. J., Carlson C. E. and Vanderhaeghen M., Phys. Rev. Lett., 93 (2004) 122301.
[18] Rekalo M. P. and Tomasi-Gustafsson E., Eur. Phys. J. A, 22 (2004) 331; Nucl. Phys. A, $\mathbf{7 4 0}$ (2004) 271; $\mathbf{7 4 2}$ (2004) 322.
[19] Arrington J., Phys. Rev. C, 68 (2003) 034325.
[20] Glazier D. I. et al., arXiv:nucl-ex/0410026.
[21] Iachello F., Jackson A. D. and Lande A,.., Phys. Lett. B, 43 (1973) 191; F. Iachello and Q. Wan, Phys. Rev. C, 69 (2004) 055204.
[22] Lomon E. L., Phys. Rev. C, 66 (2002) 045501.
[23] Bosted P. E., Phys. Rev. C, 51 (1995) 409.
[24] Andreotti M. et al., Phys. Lett. B, 559 (2003) 20 and references herein.
[25] Antonelli A. et al., Nucl. Phys. B, 517 (1998) 3.
[26] Gauzzi P., Phys. Atom. Nucl., 59 (1996) 1382 (Yad. Fiz., 59 (1996) 1441).
[27] Brash E., Jones M., Perdrisat C. F. and Punjabi V., JLab Proposal 04-108 (2004).
[28] Tomasi-Gustafsson E. and Rekalo M. P., Phys. Lett. B, 504 (2001) 291 and references herein.
[29] Rekalo M. P., Tomasi-Gustafsson E. and Prout D., Phys. Rev. C, 60 (1999) 042202.
[30] Brodsky S. J., Carlson C. E., Hiller J. R. and Hwang D. S., Phys. Rev. D, 69 (2004) 054022.

