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# Transversity from first principles in QCD

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Summary. — Transversity observables, such as the T-odd Sivers single-spin asymmetry measured in deep inelastic lepton scattering on polarized protons and the distributions which are measured in deeply virtual Compton scattering, provide important constraints on the fundamental quark and gluon structure of the proton. In this talk I discuss the challenge of computing these observables from first principles; *i.e.*; quantum chromodynamics, itself. A key step is the determination of the frame-independent light-front wave functions (LFWFs) of hadrons—the QCD eigensolutions which are analogs of the Schrödinger wave functions of atomic physics. The lensing effects of initial-state and final-state interactions, acting on LFWFs with different orbital angular momentum, lead to T-odd transversity observables such as the Sivers, Collins, and Boer-Mulders distributions. The lensing effect also leads to leading-twist phenomena which break leading-twist factorization such as the breakdown of the Lam-Tung relation in Drell-Yan reactions. A similar rescattering mechanism also leads to diffractive deep inelastic scattering, as well as nuclear shadowing and non-universal antishadowing. It is thus important to distinguish "static" structure functions, the probability distributions computed the target hadron's light-front wave functions, versus "dynamical" structure functions which include the effects of initial- and final-state rescattering. I also discuss related effects such as the J = 0 fixed pole contribution which appears in the real part of the virtual Compton amplitude. AdS/QCD, together with "Light-Front Holography", provides a simple Lorentz-invariant color-confining approximation to QCD which is successful in accounting for light-quark meson and baryon spectroscopy as well as hadronic LFWFs.

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### 1. – Introduction

"Transversity" in hadron physics encompasses the entire range of spin, orbital angularmomentum, and transverse-momentum measures of hadron structure which are accessible by experiment [1-6]. As we have seen at this meeting, highly sensitive experiments such as HERMES at DESY [7], COMPASS [8-10] at CERN, and CLAS at Jefferson Laboratory [11, 12] are now providing an extensive range of experimental results which give new insight into the fundamental quark and gluon structure of the nucleons. The challenge for theory is to synthesize this information into a consistent picture of hadron dynamics and to confront QCD at a fundamental level.

In the case of atomic physics the structure of atoms is described by Schrodinger and Dirac wavefunctions. In QCD, the corresponding relativistic, frame-independent bound state amplitudes which describe the hadron's spin and momentum structure are the *n*-particle light-front Fock state wavefunctions  $\Psi_n^H(x_i, \vec{k}_{\perp i}, \lambda_i) = \langle \Psi | n \rangle$  defined at fixed light-front time  $\tau = t + z/c$ . The constituents have light-front momentum fractions  $x_i = k^+/P^+$  with  $\sum_i^n x_i = 1$ , transverse momenta  $\vec{k}_{\perp i}$  (with  $\sum_i^n \vec{k}_{\perp i} = 0$ ) parton spin-projections  $\lambda_i$ . Remarkably, the LFWFs  $\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$  are independent of the hadron's momentum  $P^+ = P^0 + P^z$  and  $\vec{P}_{\perp}$  and thus are independent of the observer's Lorentz frame. The LFWFs are the coefficients of the expansion of a hadron eigenstate projected on a free Fock basis. The sum includes the valence Fock state and higher Fock states with sea quark-antiquark pairs and gluons. The total angular momentum  $J^z = \sum_i^n S_i^z + \sum_i^{n-1} L_i^z$  is conserved in the LF formalism by every QCD interaction and within every Fock state, just as in atomic physics. (Note that there are only n-1 independent orbital angular momenta for the *n*-parton state). The light-front formalism thus provides a consistent, frame-independent definition of quark orbital angular momentum in hadrons.

The LFWF for a hadron H is the eigensolution of the QCD light-front Hamiltonian satisfying the Heisenberg matrix equation  $H_{QCD}^{LF}|\Psi_H\rangle = M_H^2|\Psi_H\rangle$  where  $H_{QCD}$  is derived directly from the QCD Lagrangian [13]. The eigenvalues  $M_H^2$  give the discrete and continuum hadron spectrum. If one chooses to quantize QCD in light-cone gauge  $A^+ = 0$ , the gluons have physical polarization  $J^z = \pm 1$  and ghost states with negative norm are avoided. QCD(1+1) is solvable using matrix diagonalization for any number of colors, quark flavors and masses [14], using the discretized light-front quantization method [15]. More generally, the LF Hamiltonian methods provide a frame-independent nonperturbative method for solving QCD(3+1) in Minkowski space without fermion doubling. The anomalous gravitomagnetic moment of each LF Fock state vanishes [16]. as required by the equivalence theorem of gravity [17].

Given the frame-independent light-front wave functions  $\psi_{n/H}(x_i, \bar{k}_{\perp i}, \lambda_i)$ , one can compute virtually all exclusive and inclusive hadron observables. See fig. 1. For example, the valence, sea-quark and gluon distributions are defined from the squares of the LFWFS summed over all Fock states n. Form factors, exclusive weak transition amplitudes [18] such as  $B \to \ell \nu \pi$ , and the generalized parton distributions [19] such as E and H measured in deeply virtual Compton scattering are (assuming the "handbag" approximation) overlaps of the initial and final LFWFS with n = n' and n = n' + 2(ERBL contributions). The hadron's distribution amplitude  $\phi(x.Q)$  is the integral of the valence light front wave function in light-cone gauge integrated over transverse momenta  $k_{\perp}^2 < Q^2$ . ERBL and DGLAP evolution are automatically satisfied. Transversity observables can be computed from the LFWFS. In the case of pseudo-T-odd observables, one must include the lensing effect of final state or initial state interactions.

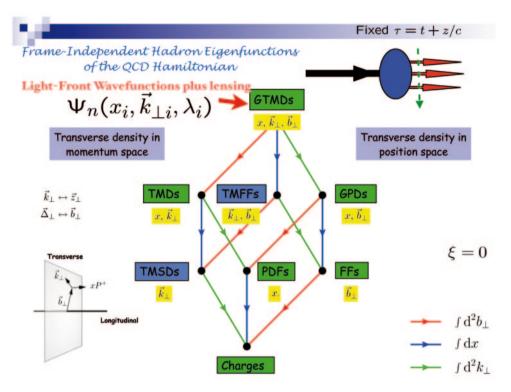


Fig. 1. – Transversity observables computable from first principles from hadron LFWFs plus lensing functions. This figure was adapted from an illustration by F. Lorcé.

The LFWFs are built as creation operators on the light-front vacuum, which unlike the usual "instant form" vacuum, is causally-connected, frame-independent, and trivial. Normal-ordering of the vacuum is thus not needed. The LF as well as the Bethe-Salpeter formalism thus predict zero cosmological constant [20, 21]. In the front form, only constituents with positive  $k^+$  occur. Thus form factors are simple overlaps of LFWFs. In contrast, in the instant form defined at fixed time t, one must include contributions to the current from vacuum fluctuations such as  $q\bar{q}g$  currents which connect to the hadron, One must also boost the equal-time wave functions, a complicated dynamical problem [22].

The five-quark Fock state of the proton's LFWF  $|uudQ\bar{Q}\rangle$  is the primary origin of the sea quark distributions of the proton [23,24]. Experiments show that the sea quarks have remarkable nonperturbative features, such as  $\bar{u}(x) \neq \bar{d}(x)$ , an intrinsic strangeness [25] distribution s(x) at x > 0.1, as well as intrinsic charm and bottom distributions at large x. Such distributions [26,27] will arise rigorously from  $gg \rightarrow Q\bar{Q} \rightarrow gg$  insertions connected to the valence quarks in the proton self-energy; in fact, they fit a universal intrinsic quark model [28] as shown by Chang and Peng [29].

### 2. – AdS/QCD and Light-Front Holography

A long-sought goal in hadron physics is to find a simple analytic first approximation to QCD analogous to the Schrödinger-Coulomb equation of atomic physics. This problem is particularly challenging since the formalism must be relativistic, color-confining,

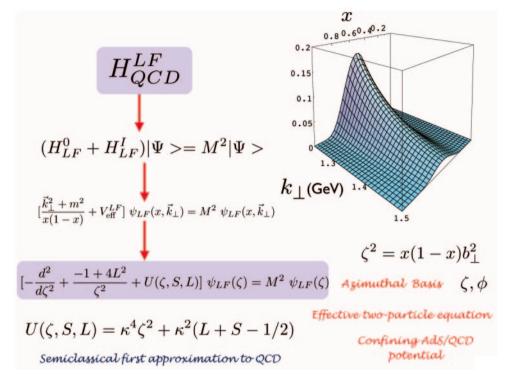


Fig. 2. – Reduction of the Light-Front Hamiltonian to an effective LF Schrödinger Equation for mesons. The insert shows the AdS/QCD light-front holography prediction for the pion's valence LFWF  $\psi(x, \vec{k}_{\perp})$ . From ref. [30].

and consistent with chiral symmetry. de Teramond and I [30] have shown that the soft-wall AdS/QCD model, modified by a positive-sign dilaton metric, leads to a simple Schrödinger-like light-front wave equation and a remarkable one-parameter description of nonperturbative hadron dynamics [30-32]. The model predicts a zero-mass pion for massless quarks and a Regge spectrum of linear trajectories with the same slope in the (lead-ing) orbital angular momentum L of the hadrons and their radial quantum number N.

Light-Front Holography maps the amplitudes which are functions of the fifth dimension variable z of anti-de Sitter space to a corresponding hadron theory quantized on the light front. The resulting Lorentz-invariant relativistic light-front wave equations are functions of an invariant impact variable  $\zeta$  which measures the separation of the quark and gluonic constituents within the hadron at equal light-front time. The result is a semi-classical frame-independent first approximation to the spectra and light-front wave functions of meson and baryon light-quark bound states, which in turn predicts the behavior of the pion and nucleon form factors [33]. The theory implements chiral symmetry in a novel way: the effects of chiral symmetry breaking increase as one goes toward large interquark separation, consistent with spectroscopic data, The hadron eigenstates generally have components with different orbital angular momentum; *e.g.*, the proton eigenstate in AdS/QCD with massless quarks has  $L^z = 0$  and  $L^z = 1$  light-front Fock components with equal probability – the proton acts as a chiral dual. Thus in AdS/QCD the spin of the proton is carried by the quark orbital angular momentum:  $J^z = \langle L^z \rangle = \pm 1/2$  since  $\sum S_q^z = 0$ , helping to explain the "spin-crisis".

The AdS/QCD soft-wall model also predicts the form of the non-perturbative effective coupling  $\alpha_s^{AdS}(Q)$  and its  $\beta$ -function [34], and the AdS/QCD light-front wave functions also lead to a method for computing the hadronization of quark and gluon jets at the amplitude level [35]. In general the QCD Hamiltonian can be systematically reduced to an effective equation in acting on the valence Fock state. This is illustrated for mesons in fig. 2 The kinetic energy contains a term  $-1 + 4L^2/\zeta^2$  analogous to  $\ell(\ell+1)/r^2$  in nonrelativistic theory, where the invariant  $\zeta^2 = x(1-x)b_{\perp}^2$  is conjugate to the  $q\bar{q}$  invariant mass  $k_{\perp}^2/x(1-x)$ . It plays the role of the radial variable r. Here  $L = L^z$  is the projection of the orbital angular momentum appearing in the  $\zeta, \phi$  basis. In QCD, the interaction U couples the valence state to all Fock states. The AdS/QCD model has the identical structure as the reduced form of the LF Hamiltonian, but it also specifies the confining potential as  $U(\zeta, S, L) = \kappa^4 \zeta^2 + \kappa^2 (L + S - 1/2)$ . This correspondence, plus the fact that one can match the AdS/QCD formulae for elastic electromagnetic and gravitational form factors to the LF Drell-Yan West formula, is the basis for light-front holography. The light-quark meson and baryon spectroscopy is well described taking the mass parameter  $\kappa \simeq 0.5 \,\text{GeV}$ . The linear trajectories in  $M_H^2(n,L)$  have the same slope in L and n, the radial quantum number. The corresponding LF wave functions are functions of the offshell invariant mass. AdS/QCD, together with Light-Front Holography [30] thus provides an simple Lorentz-invariant color-confining approximation to QCD which is successful in accounting for light-quark meson and baryon spectroscopy as well as their LFWFs. It can be systematically improved by Lippmann-Schwinger methods [36] or using the AdS/QCD orthonormal basis to diagonalize  $H_{LF}^{QCD}$  [37].

### 3. – The real part of the DVCS amplitude

It is usually assumed that the imaginary part of the deeply virtual Compton scattering amplitude is determined at leading twist by generalized parton distributions, but that the real part has an undetermined "*D*-term" subtraction. In fact, the real part is determined by the local two-photon interactions of the quark current in the QCD lightfront Hamiltonian [38, 39]. This contact interaction leads to a real energy-independent contribution to the DVCS amplitude which is independent of the photon virtuality at fixed t. The interference of the timelike DVCS amplitude with the Bethe-Heitler amplitude leads to a charge asymmetry in  $\gamma p \rightarrow \ell^+ \ell^- p$  [39-41]. Such measurements can verify that quarks carry the fundamental electromagnetic current within hadrons.

### 4. – Lensing and the Sivers effect

The effects of final-state interactions of the scattered quark in deep inelastic scattering have been traditionally assumed to be power-law suppressed. In fact, the final-state gluonic interactions of the scattered quark lead to a T-odd non-zero spin correlation of the plane of the lepton-quark scattering plane with the polarization of the target proton [42]. This leading-twist Bjorken-scaling "Sivers effect" is nonuniversal since QCD predicts an opposite-sign correlation [43, 44] in Drell-Yan reactions due to the initialstate interactions of the annihilating antiquark. The same final-state interactions of the struck quark with the spectators [45] also lead to diffractive events in deep inelastic scattering (DDIS) at leading twist, such as  $\ell p \to \ell' p' X$ , where the proton remains intact and isolated in rapidity; in fact, approximately 10% of the deep inelastic lepton-proton scattering events observed at HERA are diffractive [46,47]. The presence of a rapidity gap between the target and diffractive system requires that the target remnant emerges in a

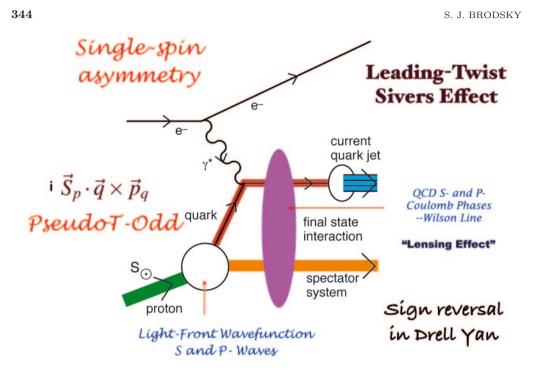


Fig. 3. – Origin of the Sivers single-spin asymmetry in deep inelastic lepton scattering.

color-singlet state; this is made possible in any gauge by the soft rescattering incorporated in the Wilson line or by augmented light-front wave functions [48].

The calculation of the Sivers single-spin asymmetry in deep inelastic lepton scattering is illustrated in fig. 3. The analysis requires two different orbital angular-momentum components: S-wave with the quark-spin parallel to the proton spin and P-wave for the

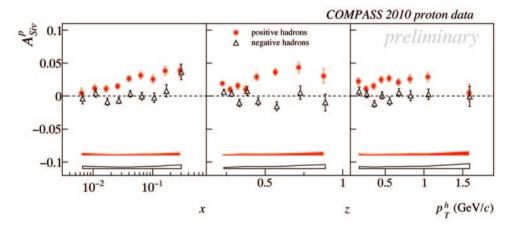


Fig. 4. – Preliminary measurements of the Sivers single-spin asymmetry by COMPASS in deep inelastic muon-proton scattering.

quark with anti-parallel spin; the difference between the final-state "Coulomb" phases leads to the  $\vec{S} \cdot \vec{q} \times \vec{p}$  correlation of the proton's spin with the virtual photon-to-quark production plane. Recent high precision measurements presented at Transversity 2011 by the COMPASS Collaboration from  $\mu p \rightarrow \mu' H^{\pm} X$  is shown in fig. 4. The original model calculation by Hwang, Schmidt, and myself [45] in fact gives a good representation of the HERMES and COMPASS data. The same S- and P-wave proton wave functions appear in the calculation of the Pauli form factor quark-by-quark. Thus one can correlate the Sivers asymmetry for each struck with the anomalous magnetic moment of the proton carried by that quark [49], thus leading to the prediction that the Sivers effect is larger for positive pions.

The empirical evidence that the Sivers effect is small for the deuteron suggests that gluons do not carry significant orbital angular momentum in the nucleon.

One also can associate the dynamics of lensing with a Wilson line for each partial wave [48]. The physics of the lensing dynamics involves nonperturbative quark-quark interactions at small momentum transfer, not the hard scale  $Q^2$  of the virtuality of the photon. It would interesting to see if these strength soft initial or final-state scattering interactions can be predicted using the confining potential of AdS/QCD.

### 5. – Dynamic versus static hadronic structure functions

The nontrivial effects from rescattering and diffraction highlight the need for a fundamental understanding the dynamics of hadrons in QCD at the amplitude level. This is essential for understanding phenomena such as the quantum mechanics of hadron formation, the remarkable effects of initial and final interactions, the origins of diffractive phenomena and single-spin asymmetries, and manifestations of higher-twist semi-exclusive hadron subprocesses.

It is natural to assume that the nuclear modifications to the structure functions measured in deep inelastic lepton-nucleus and neutrino-nucleus interactions are identical; in fact, the Gribov-Glauber theory predicts that the antishadowing of nuclear structure functions is not universal, but depends on the quantum numbers of each struck quark and antiquark [50]. This observation can explain the recent analysis of Schienbein *et al.* [51] which shows that the NuTeV measurements of nuclear structure functions obtained from neutrino charged-current reactions differ significantly from the distributions measured in deep inelastic electron and muon scattering.

As noted by Collins and Qiu [52], the traditional factorization formalism of perturbative QCD fails in detail for many types of hard inclusive reactions because of initialand final-state interactions. For example, if both the quark and antiquark in the Drell-Yan subprocess  $q\bar{q} \rightarrow \mu^+\mu^-$  interact with the spectators of the other hadron, then one predicts a  $\cos 2\phi \sin^2 \theta$  planar correlation in unpolarized Drell-Yan reactions [53]. This "double Boer-Mulders effect" can account for the large  $\cos 2\phi$  correlation and the corresponding violation [54,53] of the Lam-Tung relation for Drell-Yan processes observed by the NA10 Collaboration. An important signal for factorization breakdown at the LHC will be the observation of a  $\cos 2\phi$  planar correlation in dijet production.

It is thus important to distinguish [55] "static" structure functions which are computed directly from the light-front wave functions of a target hadron from the nonuniversal "dynamic" empirical structure functions which take into account rescattering of the struck quark in deep inelastic lepton scattering. See fig. 5. The real wave functions of hadrons which underlying the static structure functions cannot describe diffractive deep inelastic scattering nor single-spin asymmetries, since such phenomena involve the complex phase

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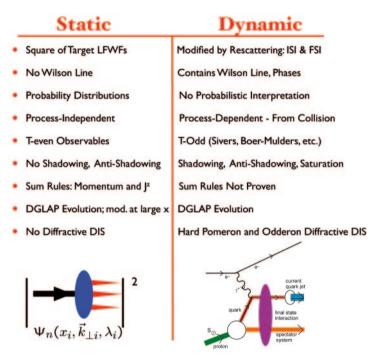


Fig. 5. – Static versus dynamic structure functions.

structure of the  $\gamma^* p$  amplitude. One can augment the light-front wave functions with a gauge link corresponding to an external field created by the virtual photon  $q\bar{q}$  pair current [56,57], but such a gauge link is process dependent [43], so the resulting augmented wave functions are not universal [45, 56, 58]. The physics of rescattering and nuclear shadowing is not included in the nuclear light-front wave functions, and a probabilistic interpretation of the nuclear DIS cross section is thus precluded.

### 6. – Transversity in Hadron-Hadron Scattering

A historic example of transversity is the remarkably large spin correlation  $A_{NN}$  measured in elastic pp elastic scattering [59] measured by Krisch and collaborators, where the beam and target are polarized normal to the scattering plane. Remarkably the ratio of spin parallel to anti-parallel scattering reaches 4:1 at  $\sqrt{s} \simeq 5$  GeV. This can be explained [60] as due to the excitation of a *uuduudcc* resonance with J = L = S = 1 in the intermediate state. A comparable effect is also seen at the  $\phi$  threshold.

## 7. – Conclusions

Transversity observables, such as the T-odd Sivers effect measured in deep inelastic lepton scattering on polarized protons and the momentum distributions measured in deeply virtual Compton scattering are now providing new constraints on the fundamental quark and gluon structure of the proton. In this talk I have discussed the challenge of computing these observables from first principles; *i.e.*; quantum chromodynamics, itself. A key step is the determination of the frame-independent light-front wave functions

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(LFWFs) of hadrons—the analogs of the Schrödinger wave functions of atomic physics. They are the eigenstates of the QCD Hamiltonian evaluated at fixed light-front time and the fundamental amplitudes underlying hadron observables such as transverse momentum distributions, structure functions and distribution amplitudes.

The lensing effects of initial-state and final-state interactions together with the LFWFs with different orbital angular momentum lead to T-odd transversity observables such as the Sivers, Collins, and Boer-Mulders distributions. The lensing effect also leads to leading-twist phenomena which break factorization theorems, such as the break-down of the Lam-Tung relation in Drell-Yan reactions. A similar rescattering mechanism also leads to diffractive deep inelastic scattering, as well as nuclear shadowing and antishadowing. Thus one should distinguish "static" structure functions, the probability distributions computed from the square of the target light-front wave functions, versus "dynamical" structure functions which include the effects of initial- and final-state rescattering. I have also discussed related effects such as the J = 0 fixed pole contribution which appears in the real part of the virtual Compton amplitude. Remarkably, AdS/QCD, together with "Light-Front Holography" provides an simple Lorentz-invariant color-confining approximation to QCD which is successful in accounting for light-quark meson and baryon spectroscopy as well as the QCD dynamics expressible in terms of their LFWFs.

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