# Cluster structure of neutron-rich ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$ via resonant alpha scattering 

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#### Abstract

Summary. - Neutron-rich ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$ nuclei were studied via resonant $\alpha$ scattering of radioactive ${ }^{6} \mathrm{He}$ and ${ }^{10} \mathrm{Be}$ beams, respectively, produced by the TwinSol facility at the University of Notre Dame. The Prototype Active-Target Time-Projection Chamber (pAT-TPC) was used as a thick gaseous $\alpha$ target to induce resonant scattering and as a device to track reacted particles inside the target, providing continuous excitation functions and angular distributions over a wide range of energies and angles. The experimental results indicate a melting phenomenon of $\alpha$ clusters in the $4^{+}$rotational member of the ${ }^{10} \mathrm{Be}$ ground state and a linear chain alignment of three $\alpha$ clusters in ${ }^{14} \mathrm{C}$ excited states, as recently predicted by an anti-symmetrized molecular dynamics calculation.


## 1. - Introduction

Studies of $\alpha$ clustering, dated back to as far as the 1930s [1], still constitute the forefront in modern nuclear physics. Neutron-rich nuclei have increasingly attracted attention in recent years. If clustering occurs, these nuclei represent a hybrid system, where excess neutrons around $\alpha$ clusters add another degree of freedom, prompting questions on whether $\alpha$ clusters in stable nuclei with equal numbers of protons $(Z)$ and neutrons $(N)$ persist as they are, or change their cluster properties such as geometrical alignment, or even dissolve into a shell-model-like state. Neutron-rich ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$ are very important nuclei to answer these questions since their $N=Z$ isotopes, ${ }^{8} \mathrm{Be}$ and ${ }^{12} \mathrm{C}$, have arguably the best established cluster states, that are even reproduced by ab initio calculations using bare nuclear forces [2,3]. Previous theoretical studies by the molecular
orbital model [4], the anti-symmetrized molecular dynamics (AMD) approach [5-7], the multicluster generator coordinate method [8], and full [9,10] or semi microscopic cluster models [11] show that the two valence neutrons of ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$ significantly impact the $\alpha$ clustering, predicting molecular neutron orbitals [4], or linear chain alignment of $\alpha$ clusters [7], the phenomenon that was first conjectured for the $N=Z$ nuclei [12], but remains unidentified even for the simplest $3 \alpha$ case in ${ }^{12} \mathrm{C}[13,14]$. While a number of experiments have been carried out [15-22], most of the predicted cluster states remain unknown or to be studied.

We studied ${ }^{10} \mathrm{Be}[23]$ and ${ }^{14} \mathrm{C}[24]$ via $\alpha$ resonant scattering off radioactive ${ }^{6} \mathrm{He}$ and ${ }^{10}$ Be beams, respectively. The active target and time-projection chamber, Prototype AT-TPC (pAT-TPC) [25] containing He and $\mathrm{CO}_{2}$ gas mixture was used as a reaction target as well as tracking medium of charged particles. The thick target method [26], where excitation functions are measured by decelerating beam particles over the length of a thick target, was used. Measuring reaction trajectories inside the target, commonly called active target technique [27], allows one to directly determine the reaction vertex and unambiguously deduce the beam energy, which translates into the resonance energy $[23,24,28]$. This would otherwise be limited with the widely-used multiple silicon detector setup that indirectly determines the reaction vertex, by assuming reaction kinematics energetically allowed, from the energy and angle of an $\alpha$ particle after leaving the target. The active target method enables the measurement of wide-ranging and continuous excitation functions and angular distributions, facilitating the identification of unknown resonances and oscillatory diffraction patterns, which are the most reliable information in determining the spin and parity.

## 2. - Experiment

These measurements were performed as the first series of experiments of the pAT-TPC using TwinSol [29] radioactive-ion beams at the FN tandem accelerator facility of the University of Notre Dame [30]. ${ }^{6} \mathrm{He}$ ions were produced via the $\left(d,{ }^{3} \mathrm{He}\right)$ reaction using a deuterium target at $1200 \mathrm{~mm}-\mathrm{Hg}$ and $29.2 \mathrm{MeV}{ }^{7} \mathrm{Li}(3+)$ primary beam. To produce ${ }^{10} \mathrm{Be}$ ions, a stack of four $0.1 \mathrm{mg} / \mathrm{cm}^{2}$ thick ${ }^{13} \mathrm{C}$ targets were bombarded by a $46 \mathrm{MeV}{ }^{11} \mathrm{~B}(5+)$ primary beam. Radioactive ions thus produced were collected and purified in flight by the TwinSol device [29] consisting of a pair of solenoidal magnets. The secondary beam was delivered to the cylindrical target volume of $\mathrm{He}: \mathrm{CO}_{2} 90: 10$ mixture gas at 1 atm of the pAT-TPC [25], measuring 50 cm along the beam axis and 27 cm in diameter. The beam energies of ${ }^{6} \mathrm{He}$ and ${ }^{10} \mathrm{Be}$ were 15 and 40 MeV , respectively. The corresponding center-of-mass energies $E_{\text {c.m. }}$ ( 6 MeV for ${ }^{6} \mathrm{He}$ and 11.3 MeV for ${ }^{10} \mathrm{Be}$ ) decreased to zero while travelling the length of the gas volume. The average rate of ${ }^{6} \mathrm{He}$ that entered the volume was $2 \times 10^{3}$ ions per second with a purity of $90 \%$. The main impurity was ${ }^{4} \mathrm{He}$. The average rate of ${ }^{10} \mathrm{Be}$ was $10^{3}$ ions per second. The beam purity was about $35 \%$ with main contaminants of ${ }^{4} \mathrm{He}(2+)(50 \%),{ }^{9} \mathrm{Be}(4+)(5 \%)$, and ${ }^{10} \mathrm{~B}(4+)(3 \%)$. Electrons from reaction trajectories are guided toward the Micromegas amplifier [31] by an electric field of $0.8 \mathrm{kV} / \mathrm{cm}$ parallel to the beam axis. The Micromegas consists of 2 mm wide radial strips separated into quadrants. A waveform digitizer [32] records the charge as a function of drift time over $40 \mu$ s by using an array of 511 switching capacitors.


Fig. 1. - (A) Excitation function for ${ }^{6} \mathrm{He}+\alpha$ elastic scattering. The data are integrated over $\theta_{\text {c.m. }}=65^{\circ}-135^{\circ}$. The observed $4^{+}$resonance at around $E_{\text {c.m. }}=2.7 \mathrm{MeV}$ and the missing $4^{+}$ resonance expected from a ${ }^{10} \mathrm{Be}$ state at $E_{\mathrm{x}}=11.8 \mathrm{MeV}$ are denoted by the lines. (B) Differential cross sections of ${ }^{6} \mathrm{He}+\alpha$ elastic scattering for the $4^{+}$resonance at $E_{\mathrm{c} . \mathrm{m} .}=2.7 \mathrm{MeV}$ (filled circles). Off-resonance data at 3.3 MeV (open circles) are also shown for reference. The oscillatory pattern of the 2.7 MeV data agrees with that of the squared Legendre function with $L=4$ (dashed line), for which an arbitrary scaling factor was adopted for presentation purposes. (C) Excitation energies vs. $J(J+1$ ) plot for rotational band members of the ground (circles) and second (squares) $0^{+}$states of ${ }^{10} \mathrm{Be}$. The ground-state band members of ${ }^{8} \mathrm{Be}$ (triangles) are also shown for comparison.

## 3. - Results

The angle-integrated excitation function for ${ }^{6} \mathrm{He}$ elastic scattering is shown in fig. 1(A). While elastic scattering was previously measured at several beam energies $[15-17,19]$, this is the first differential cross section data taken continuously over a finite range of energy. The resonance visible at $E_{\text {c.m. }}=2.56(15) \mathrm{MeV}$ is assigned a spin and parity of $4^{+}$from the diffraction seen in the angular distribution of fig. 1(B), which excellently agrees with the oscillatory pattern of the squared Legendre function for an angular momentum $L=4$. The partial $\alpha$ decay width was estimated to be $\Gamma_{\alpha} / \Gamma=0.49(5)$ from the resonance cross sections. These results are in line with the previous measurement with a narrower energy range, but with better statistics [19]. The large partial width of this $4^{+}$state, widely considered as the $4^{+}$member of the second $0^{+}$rotational band, supports the predicted $\sigma$-type molecular orbital structure around the two $\alpha$ clusters $[4,5]$. Another $4^{+}$state of the ground state $0^{+}$band, often discussed as a $\pi$-type partner of the second $0^{+}$band, is predicted at $E_{\text {c.m. }}=3$ to 6 MeV by several calculations $[4-6,8,10,11]$. This state has been associated with a ${ }^{10} \mathrm{Be}$ level found at an excitation energy $\left(E_{\mathrm{x}}\right)$ of $11.76 \mathrm{MeV}[20]$, or $E_{\mathrm{c} . \mathrm{m} .}=4.36 \mathrm{MeV}$, given the $\alpha$ emission threshold at $E_{\mathrm{x}}=7.4 \mathrm{MeV}$. However, our result that allowed us to survey a wide range of excitation energies up to $E_{\text {c.m. }}=6 \mathrm{MeV}$ rules out resonances at predicted energies, with an upper limit of $\Gamma_{\alpha}=20 \mathrm{keV}$. This is almost one order of magnitude small than that of the 2.56 MeV resonance with $\Gamma_{\alpha}=145(15) \mathrm{keV}$. The missing resonance strength and the hindered branching for $\alpha$ emission indicate that the degree of clusterization is reduced in the $4^{+}$state of the ground state $0^{+}$rotational band. The weakening of clustering is pointed out by an early AMD study of ${ }^{10} \mathrm{Be}$ [5], predicting that the $\alpha$ clusters in the $0^{+}$ground state gradually dissolve in the rotational band members as the total spin increases. It is interesting to note that the ground state band of ${ }^{10} \mathrm{Be}$ has almost the same level spacing as ${ }^{8} \mathrm{Be}$ (fig. $1(\mathrm{C})$ ), while the $\alpha$ clustering in ${ }^{8} \mathrm{Be}$ appears to be robust in $0^{+}, 2^{+}$, and $4^{+}$states. The $\alpha$ spectroscopic factors of ${ }^{8} \mathrm{Be}$ are equally large in all of


Fig. 2. - (A) Excitation function for ${ }^{10} \mathrm{Be}+\alpha$ elastic scattering. Resonances of ${ }^{14} \mathrm{C}$ and their spins and parities from the present analysis are shown. (B) Differential cross sections of ${ }^{10} \mathrm{Be}+\alpha$ elastic scattering for the resonance at $E_{\mathrm{c} . \mathrm{m} .}=7.0 \mathrm{MeV}$ (filled circles). The oscillatory pattern agrees with that of the squared Legendre function with $L=4$ (dashed line), for which an arbitrary scaling factor was used. (C) Comparison of the $2^{+}$and $4^{+}$resonance energies to the linear $3 \alpha$ chain states predicted in a $\beta-\gamma$ constraint AMD study [7]. The proton $\left(\rho_{p}\right)$ and neutron $\left(\rho_{n}\right)$ density distributions and their differential $\left(\Delta \rho=\rho_{p}-\rho_{n}\right)$ for the predicted linear chain states are displayed.
these states according to the folding-model potential calculation that well describes the level energies and widths of these states [33]. In one ab initio Quantum Monte Carlo calculation of ${ }^{8} \mathrm{Be}[2]$, the density distribution of the $4^{+}$state shows the two $\alpha$ clusters as clearly as in the $0^{+}$ground state. The dissociation of $\alpha$ clusters in ${ }^{10} \mathrm{Be}$, which thus stands in stark contrast with ${ }^{8} \mathrm{Be}$, may be due to the two excess neutrons that complete the filling of the $1 p_{3 / 2}$ orbital. The large energy gap relative to the higher $1 p_{1 / 2}$ orbital that gives rise to the subshell closure at $N=6$ may favour shell-model-like structure over the $\alpha$ clustering.

The excitation function for elastic $\alpha$ scattering of ${ }^{10} \mathrm{Be}$ is shown in fig. 2(A). Among several resonances of ${ }^{14} \mathrm{C}$ identified, there are two positive-parity states, one being a $2^{+}$state at $E_{\text {c.m. }}=3.0 \mathrm{MeV}$, the other a $4^{+}$state at 7.0 MeV . These spin and parity assignments were made again from the oscillation patterns of differential cross sections (fig. 2(B)). These levels are compared to a $\beta-\gamma$ constraint AMD calculation using the generator coordinator method [7] in fig. 2(C). The experimental resonance energies well agree with the $2^{+}$and $4^{+}$states of one of the rotational bands predicted. As seen in the intrinsic density distributions, three $\alpha$ clusters are aligned in a linear arrangement in this band. This supports the presence of a linear $3 \alpha$ chain structure in excited states of ${ }^{14} \mathrm{C}$.

## 4. - Summary

To study the cluster structure of ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$, resonant $\alpha$ scattering of radioactive ${ }^{6} \mathrm{He}$ and ${ }^{10} \mathrm{Be}$ beams was measured at the TwinSol facility using the pAT-TPC. The hindered branching for $\alpha$ emission observed for the $4^{+}$rotational member of the ${ }^{10} \mathrm{Be}$ ground state indicates that the $\alpha$ clustering of the ground state, consistently predicted by different theoretical studies, fades away in the $4^{+}$rotational member. The newly-found $2^{+}$and $4^{+}$states of ${ }^{14} \mathrm{C}$ agree with linear chain states predicted by the recent AMD work. The $\alpha$ clustering is robust against dissociation in ${ }^{8} \mathrm{Be}$ and the linear chain structure is predicted to be manifested very weakly in ${ }^{12} \mathrm{C}$. The present results suggesting these phenomena realized in ${ }^{10} \mathrm{Be}$ and ${ }^{14} \mathrm{C}$ indicate that two valence neutrons alone can drastically and essentially evolve the $\alpha$ cluster structure.

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