

## Configuration mixing investigation in germanium isotopes through measurement of $E0$ transition strengths

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**Summary.** — Experimental and theoretical studies of the germanium isotopes on the neutron-rich side of the stability valley point increasingly toward the emergence of triaxiality, configuration mixing, and shape coexistence phenomena. Studies of the  $E0$  strengths, which can provide a direct measure of the amount of configuration mixing, are lacking. Thus, determining  $E0$  transition strengths is essential for an understanding of the evolution of structures in the Ge isotopes. Beta-decay experiments populating excited states in the  $^{72,74,76,78}\text{Ge}$  isotopes were performed at the TRIUMF-ISAC radioactive beam facility. Gamma-ray and electron spectroscopic investigations have been performed, to measure  $E0$  strengths between states of  $J > 0$ , exploiting the GRIFFIN spectrometer combined with the PACES silicon detector array. Preliminary results from this study are presented.

## 1. – Introduction

The structure of Ge isotopes ( $Z = 32$ ) has been widely investigated both theoretically and experimentally over the years, and indications of shape coexistence, triaxiality and configuration mixing have been found [1-4]. The energy systematics of the first excited  $0^+$  state of the even-even Ge nuclei around stability varies parabolically and comes to a minimum for  $^{72}\text{Ge}$  ( $N = 40$ ), as can be observed in fig. 1. In particular, in  $^{72}\text{Ge}$  the  $0_2^+$  is the very first excited state. Evidence of strong mixing between the ground state and first excited  $0^+$  state in this nucleus has been drawn from transfer reaction studies, while indications of a weakening of the mixing for the higher mass cases have been found [1]. Moreover, a recent Coulomb excitation study led to the conclusion that the ground state and first excited  $0^+$  states of  $^{72}\text{Ge}$  could be well described via an admixture of two triaxial rotors [3].

Electric monopole ( $E0$ ) transition strengths,  $\rho^2(E0)$ , can probe the configuration mixing of the initial and final states considered [5]. However, only a few  $E0$  strengths have

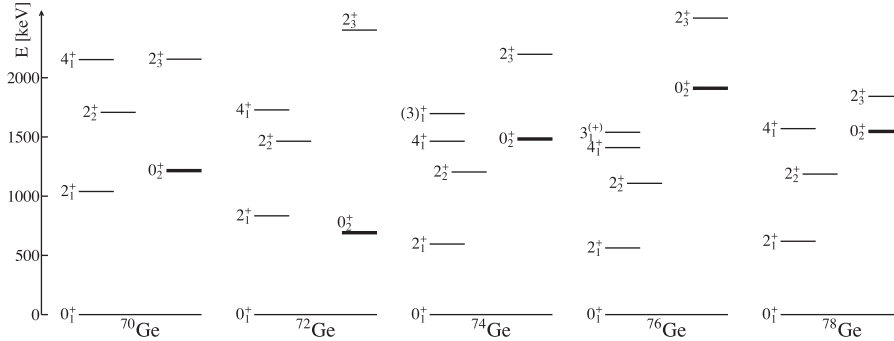


Fig. 1. – Partial decay schemes of even-even Ge isotopes with mass  $A = 70$  to  $78$  [6-10]. The excited  $0^+$  states are highlighted in bold.

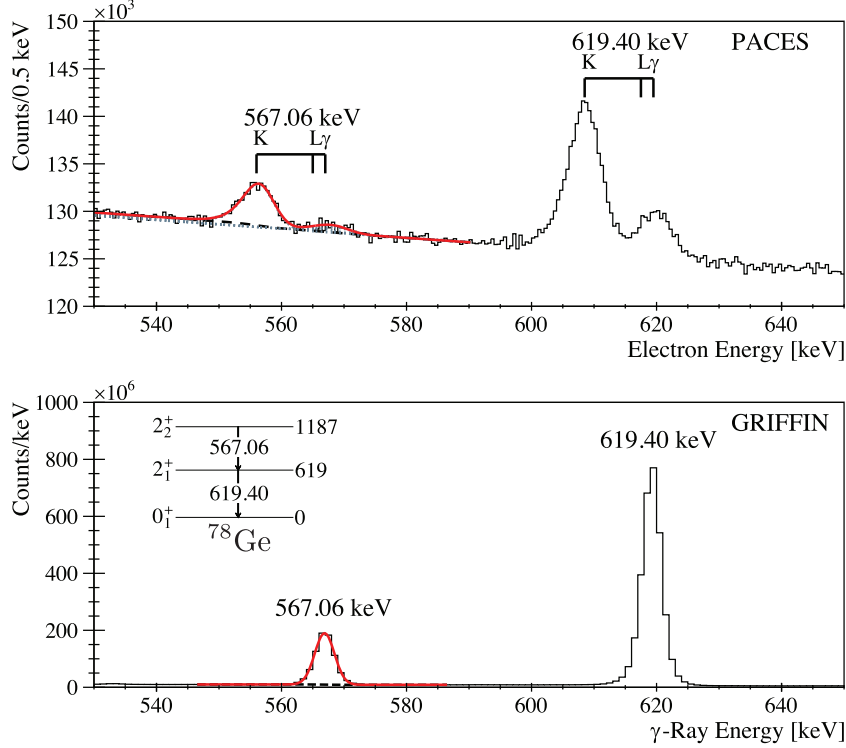


Fig. 2. – Comparison of the spectra recorded with one PACES crystal (top) and the GRIFFIN spectrometer (bottom) for the  $^{78}\text{Ge}$  isotope in the 2019 experiment. In the PACES spectrum, a fit of the K-shell, L-shell and photo-peak components of the 567-keV,  $2_2^+ \rightarrow 2_1^+$  transition is shown. Note that the background includes contributions from  $\beta$  particles and the Compton continuum of  $\gamma$  rays. The spectrum shown is recorded in singles, hence there is no background subtraction. In the GRIFFIN spectrum, a fit of the photo-peak of the same transition is shown. A partial level scheme of  $^{78}\text{Ge}$  indicates the relevant transitions.

been measured in the Ge isotopic chain so far [11]. Therefore, an experimental determination of  $E0$  transition strengths is needed for a systematic investigation of configuration mixing along the chain.

This experimental work focused on the even-even Ge isotopes with mass  $A = 72$  to  $78$ . Such nuclei were populated through beta-decay experiments. The experimental details are briefly described in the following section. The last section of this paper summarizes the results of the analysis performed.

## 2. – Experiment and analysis

The experiments were performed at the Isotope Separator and Accelerator (ISAC) facility [12] at the TRIUMF laboratory in Vancouver, Canada, in 2017 and 2019. The four isotopes of interest,  $^{72,74,76,78}\text{Ge}$ , were populated through the  $\beta^-$  decay of the corresponding Ga isobars, that were delivered as beams to the center of the GRIFFIN  $\beta$ -decay station [13]. The radioactive Ga beams were produced through the ISOL technique.

The  $\gamma$ -ray and internal conversion decay of the Ge isotopes under investigation were measured by the high-efficiency and high-resolution GRIFFIN  $\gamma$ -ray spectrometer and its

ancillary detector PACES. GRIFFIN was composed of 15 high-purity Ge clover detectors, while PACES comprised five lithium-drifted silicon [Si(Li)] crystals.

To determine the  $\rho^2(E0)$  value for the  $2_2^+ \rightarrow 2_1^+$  transition of the nuclei of interest, it is necessary to measure the experimental internal conversion coefficient  $\alpha$  and the  $E2/M1$  multipole mixing ratio  $\delta$  of such transition. The coefficient  $\alpha$  is a ratio of the intensity of emitted conversion electrons relative to emitted photons for a given transition. To measure the ratio of the intensities, the conversion electron spectra recorded by PACES and the  $\gamma$ -ray spectra recorded by GRIFFIN were used. Figure 2 shows both spectra for the case of  $^{78}\text{Ge}$ . Fits of the peaks corresponding to the  $2_2^+ \rightarrow 2_1^+$  transition are shown in red in the figure. A  $\gamma\gamma$  angular correlation analysis is also in progress, to provide a measurement of the  $E2/M1$  multipole mixing ratios  $\delta$ .

### 3. – Conclusions

Preliminary results from the internal conversion analysis point to the emergence of a finite  $E0$  component in the  $2_2^+ \rightarrow 2_1^+$  transition of  $^{72}\text{Ge}$ , and to a near-zero  $E0$  strength in the higher mass cases ( $^{74,76,78}\text{Ge}$ ). This result is in agreement with previous transfer reaction studies that indicated a strong configuration mixing in  $^{72}\text{Ge}$ , and a weakening of the mixing for the even-even Ge nuclei with  $N > 40$ . Currently, an effective theoretical description of  $E0$  strengths in  $J > 0$  transitions is still lacking. Therefore, further efforts on the theoretical side will be needed to provide a comprehensive description of the origin of the  $E0$  strength, as well as new experimental measurements of  $\rho^2(E0)$  that could benchmark such studies.

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